

# Shock compression of quartz in the high-pressure fluid regime

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The Hugoniot of quartz has been measured using laser-driven shock waves with pressures from 2 to 15 Mbars. Within this pressure range silica transforms from a liquid near melt into a dense plasma. Results are in good agreement with previous studies in part of this range performed using explosive- and nuclear-driven shocks indicating the absence of time-dependent effects for time scales between several hundred picoseconds and several hundred microseconds. These data combined with earlier data at lower pressures clearly show the increasing compressibility of silica as it transitions from solid to liquid to dense plasma regimes. © 2005 American Institute of Physics.

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## I. INTRODUCTION

Silica presents a prototypical system for studying high-pressure structural changes, one that is of fundamental importance to the study of the Earth's interior.<sup>1</sup> Its phase diagram, revealed by a wide array of static<sup>2–6</sup> and dynamic<sup>7–10</sup> compression experiments, shows a transformation from tetrahedral to octahedral coordination with increasing pressure, although many details remain controversial.<sup>11–13</sup> The availability of several silica polymorphs at ambient pressure—in particular—fused silica, quartz, cristobalite, coesite, and stishovite—in addition to porous samples has made dynamic compression experiments especially valuable since the different ambient densities allow shock Hugoniots to traverse a wide range of phase space.<sup>12,14</sup> While extensive shock data exist for the various solid phases of silica, only limited data<sup>15,16</sup> exist for the Hugoniot of the high-pressure fluid. Shock melting of  $\alpha$ -quartz, detected using temperature measurements, was observed at 1.1 Mbars;<sup>9</sup> above this pressure silica is expected to transform continuously from a liquid into a dense plasma, a process that has recently been investigated in molecular-dynamics simulations.<sup>17</sup> Precise measurement of the Hugoniot through this dissociation regime is fundamental to the modeling of large meteor impacts<sup>18</sup> and provides a bound on the behavior of liquid silicates that

likely exist at the Earth's core-mantle boundary.<sup>19,20</sup> Such studies are critical to developing an understanding of how covalently bonded, condensed-matter systems evolve into dense, strongly coupled plasmas at high pressure and temperature.

In this study we perform extensive measurements of the  $\alpha$ -quartz Hugoniot from 2 to 15 Mbars using laser-driven shock waves. A fundamental question that arises in dynamic compression experiments is whether the states probed are at equilibrium. This issue is of particular relevance to laser-driven shocks where ultrahigh pressures are achieved in less than a nanosecond. In comparison,<sup>21</sup> nuclear-driven shock experiments were performed over time scales of tens of microseconds,<sup>10</sup> laboratory explosive and gas gun studies over fractions of microseconds,<sup>9,10</sup> and magnetically driven flyer plates over tens of nanoseconds.<sup>22</sup> Since there exist both explosive- and nuclear-driven data on  $\alpha$ -quartz in the range of 2–6 Mbars, and also a single nuclear experiment at 20 Mbars,<sup>15,16</sup> this material presents a valuable medium for examining the validity of the equilibrium assumption in laser-driven equation-of-state (EOS) studies. Although shocked quartz has been shown to exhibit nonequilibrium behavior in its solid phases<sup>9,23</sup> we find that in the fluid regime of silica excellent agreement exists amongst these different experiments whose time scales differ by more than four orders of magnitude.

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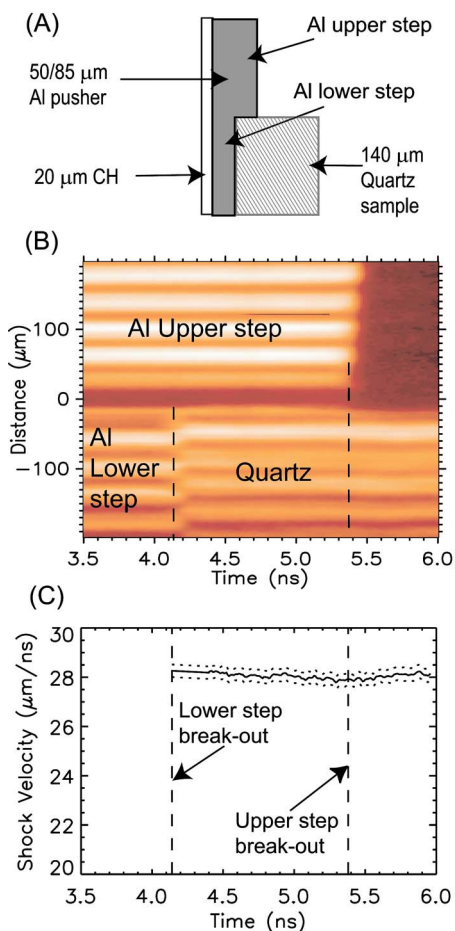


FIG. 1. (Color online) (a) Schematic of the target: drive laser is incident from the left; VISAR views from the right. (b) Streak camera record of the line-VISAR trace showing breakout from upper and lower aluminum steps and the reflecting shock wave in quartz. (c) Shock velocity in quartz inferred from the VISAR fringe shift in (b) with uncertainties given by the dotted lines.

## II. METHODS

The Hugoniot measurements in this experiment use the impedance-match technique<sup>24</sup> with aluminum as the material standard. Determining the pressure and density in the sample requires knowledge of the Hugoniot and release behavior of aluminum. This and a similar inverse approach were used in previous experiments<sup>15,16</sup> to which our data will be compared. In other respects our experiments differ significantly from the earlier ones: in both time and length scales, in the drive mechanism, and in the detector systems.

This experiment was performed on the OMEGA laser at the University of Rochester, a neodymium-doped phosphate glass system that operates with frequency-tripled, 0.35-μm light.<sup>25</sup> To generate the shock pressures explored in these experiments, laser energies of 440–3100 J were delivered using 3.7-ns square pulse. The laser focal region had a super-Gaussian distribution with a 600-μm-diam central region of uniform intensity. Targets consisted of a *z*-cut,  $\alpha$ -quartz sample mounted on the lower step of a diamond-turned aluminum pusher [see Fig. 1(a)]. A plastic ablator was used to minimize hard x-ray generation in the laser-plasma region. Three different thicknesses were used for the ablator-

pusher combination: 20 μm of CH on a 90–130-μm Al step (90-μm lower step and 130-μm upper step), 20 μm of CH on a 50–85-μm Al step and 20 μm of CH plus 80 μm of CH-Br (plastic with 2% Br by atomic weight) on a 50–85-μm Al step. The density of quartz was measured to be 2.65 g/cm<sup>3</sup> and the refractive index along its *c* axis at 532 nm was found to be 1.547. The height of the step in the aluminum pusher was measured in each target using a white-light interferometer.

The shock diagnostic was a line-imaging velocity interferometer system for any reflector<sup>26,27</sup> (VISAR) which measures the Doppler shift of a moving reflector. Implementation of this system on the OMEGA laser is described in detail in Ref. 28. Two VISAR's with different velocity sensitivities were used to resolve  $2\pi$  phase-shift ambiguities that occur at shock breakout from the aluminum. The velocity sensitivities for the two VISAR instruments, which used 7.2-mm- and 3.1-mm-thick fused silica etalons, were 4.465 and 10.400 μm/ns/fringe in quartz. Postprocessing of the VISAR images can determine the fringe position to  $\sim 5\%$  of a fringe; since the measured shock velocities are 14–24 μm/ns in quartz, the multiple fringe shifts allow the precision of the shock velocity measurement to be  $\sim 1\%$ – $2\%$ . The probe source was an injection-seeded, *Q*-switched, yttrium aluminum garnet laser, operating at a wavelength of 532 nm with a pulse length of  $\sim 25$  ns. Streak cameras with temporal windows of  $\sim 3$  ns were used to detect the reflected probe signal. The time resolution of the VISAR and streak camera system was 40–50 ps.

## III. RESULTS

A sample VISAR trace is shown in Fig. 1(b). This single time-resolved image contains the two experimental observables used to determine an impedance-matched EOS point in quartz: aluminum,  $U_s^{\text{Al}}$ , and quartz,  $U_s^{\text{Q}}$ , shock speeds. The average  $U_s^{\text{Al}}$  is determined by the transit time across the aluminum step, and the time-resolved  $U_s^{\text{Q}}$  is determined by the fringe shifts once the shock wave enters the quartz, caused by a Doppler shift at the reflecting shock front. Pressures were high enough on all shots that the shock front in quartz had reflectivities greater than a few percent.<sup>29</sup> The resulting shock velocity history in quartz is shown in Fig. 1.

Errors in  $U_s^{\text{Q}}$  are 1%–2% and are dominated by the uncertainty in determining a fringe shift as described above. Errors in  $U_s^{\text{Al}}$  are  $\sim 1.5\%$ – $2.5\%$  and give rise to the largest uncertainty in the shock density inferred by impedance matching. The primary contribution to this error comes from measuring the aluminum breakout time at each step. Typically this uncertainty is about 15–25 ps which, for the streak camera sweep speeds used in this experiment, corresponds to 5–8 pixels on the VISAR record.<sup>30</sup> For transit times ranging from 1.2 to 2.5 ns this gives an uncertainty of 1%–2%. Other components of the transit-time uncertainty include the step height measurement ( $\pm 0.2$  μm, giving  $\sim 0.6\%$  error), and streak camera sweep speed ( $\pm 0.5\%$ ), with errors summed in quadrature.

Three remaining potential sources of error in  $U_s^{\text{Al}}$ —edge rarefactions, shock nonplanarity, and shock unsteadiness—

are minimized using suitable correction procedures. Side rarefactions, which occur at the edge of the aluminum step next to the quartz sample, can perturb breakout from the top step if the measurement is taken too close to the edge. Such rarefaction waves move laterally at velocities less than the shock speed. Thus as long as breakout times from the top step are taken more than one step height ( $35\text{--}40\text{ }\mu\text{m}$ ) away from the edge such rarefaction effects are avoided. The effects of shock nonplanarity are minimized by reducing the separation between the top and bottom step breakout time measurements, while still avoiding the rarefaction region. Nonplanarity in these experiments can be described over the several hundred micron field of view by an effective shock radius of curvature of around  $4\text{ mm}$  which gives a  $1\%$  error in the velocity for lateral separations of  $50\text{ }\mu\text{m}$ . This is reduced further by tracking the spatial variation of breakout times over  $\sim 100\text{--}150\text{ }\mu\text{m}$  on the top and bottom steps and extrapolating them to the same point in the center of the edge region [the distance= $0\text{ }\mu\text{m}$  point in Fig. 1(b)]. Using this approach we estimate typical nonplanarity errors to be  $<1\%$ .

The importance of shock steadiness effects arises from the need to compare  $U_s^{\text{Al}}$  and  $U_s^{\text{Q}}$  at similar times. More specifically, correct application of the impedance-matching condition requires that  $U_s^{\text{Al}}$  and  $U_s^{\text{Q}}$  be determined at breakout from the aluminum-quartz interface ( $t_{\text{bo}}$ ). In Figs. 1(b) and 1(c), this is the dashed line at  $4.13\text{ ns}$ . Determining  $U_s^{\text{Q}}(t_{\text{bo}})$  is

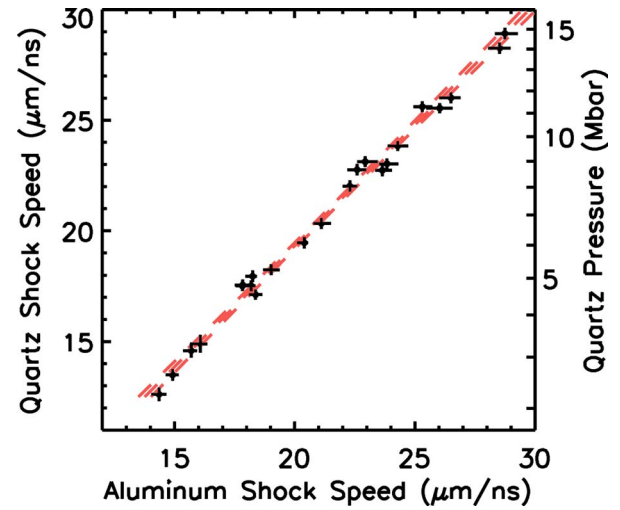


FIG. 2. (Color online) Plot of the experimental observables determined at the aluminum-quartz interface: shock velocity in the aluminum standard, as determined by the transit time across the aluminum step, vs shock velocity in quartz as measured by the VISAR. The data can be represented by a straight line with fit parameters given in the text.

straightforward and involves a linear extrapolation of data starting at  $100\text{--}200\text{ ps}$  after  $t_{\text{bo}}$ ; this minimizes uncertainties arising immediately after breakout where velocities are

TABLE I. Summary of experimental shock wave data on quartz.  $U_s^{\text{Al}}$  and  $U_s^{\text{Q}}$  are the primary experimental observables; measurement uncertainties are listed in parentheses.  $P^{\text{Q}}$ ,  $\rho^{\text{Q}}$ , and  $U_p^{\text{Q}}$  are inferred from impedance matching with aluminum; random and systematic errors for these quantities are listed in parentheses first and second, respectively. The random errors arise from the listed measurement uncertainties in the primary observables. Systematic errors arise from uncertainties in the experimentally derived aluminum Hugoniot.

Shot No.	$U_s^{\text{Al}}$ ( $\mu\text{m/ns}$ )	$U_s^{\text{Q}}$ ( $\mu\text{m/ns}$ )	$P^{\text{Q}}$ (Mbar)	$\rho^{\text{Q}}$ ( $\text{g/cm}^3$ )	$U_p^{\text{Q}}$ ( $\mu\text{m/ns}$ )
31 913	14.33(0.34)	12.62(0.32)	2.37(0.12,0.02)	6.05(0.44,0.06)	7.09(0.33,0.05)
31 917	14.88(0.30)	13.50(0.26)	2.68(0.12,0.04)	5.96(0.38,0.10)	7.49(0.33,0.10)
29 011	15.59(0.35)	14.59(0.32)	3.11(0.15,0.03)	5.90(0.40,0.07)	8.04(0.38,0.08)
29 031	15.94(0.43)	14.90(0.41)	3.30(0.19,0.03)	6.03(0.51,0.07)	8.35(0.47,0.08)
27 890	17.76(0.35)	17.56(0.26)	4.54(0.18,0.03)	5.97(0.32,0.06)	9.77(0.38,0.07)
29 411	17.82(0.29)	17.52(0.24)	4.57(0.15,0.03)	6.05(0.29,0.06)	9.84(0.32,0.07)
29 400	18.11(0.32)	17.96(0.26)	4.79(0.17,0.04)	6.03(0.31,0.06)	10.07(0.35,0.07)
29 025	18.08(0.29)	17.52(0.25)	4.70(0.15,0.03)	6.28(0.32,0.06)	10.13(0.32,0.07)
31 911	18.37(0.29)	17.13(0.23)	4.77(0.15,0.04)	6.87(0.39,0.08)	10.52(0.32,0.08)
27 898	19.03(0.34)	18.25(0.24)	5.32(0.19,0.04)	6.67(0.39,0.08)	11.00(0.38,0.08)
29 014	20.22(0.34)	19.46(0.27)	6.20(0.20,0.05)	6.94(0.40,0.09)	12.03(0.37,0.10)
29 418	21.13(0.37)	20.34(0.26)	6.92(0.23,0.06)	7.19(0.44,0.11)	12.84(0.41,0.11)
29 029	22.27(0.33)	22.02(0.26)	8.00(0.22,0.08)	7.03(0.35,0.11)	13.71(0.36,0.13)
27 900	22.56(0.43)	22.76(0.26)	8.36(0.29,0.08)	6.78(0.39,0.11)	13.86(0.47,0.14)
29 419	23.05(0.40)	23.12(0.24)	8.78(0.28,0.09)	6.97(0.38,0.12)	14.33(0.44,0.15)
29 022	23.72(0.33)	22.74(0.27)	9.12(0.23,0.10)	7.93(0.45,0.17)	15.14(0.37,0.16)
29 413	23.90(0.42)	23.03(0.24)	9.32(0.29,0.10)	7.86(0.51,0.17)	15.27(0.46,0.17)
27 896	24.27(0.45)	23.84(0.23)	9.79(0.31,0.11)	7.57(0.48,0.16)	15.50(0.49,0.17)
29 008	25.27(0.45)	25.61(0.25)	10.99(0.34,0.13)	7.21(0.41,0.15)	16.20(0.49,0.19)
27 894	25.96(0.61)	25.54(0.23)	11.48(0.46,0.14)	7.89(0.64,0.19)	16.96(0.67,0.21)
29 420	26.16(0.74)	26.01(0.25)	11.77(0.56,0.15)	7.71(0.72,0.18)	17.08(0.81,0.21)
32 250	28.49(0.49)	28.26(0.26)	14.32(0.42,0.20)	8.19(0.53,0.23)	19.12(0.54,0.27)
29 007	28.80(0.48)	28.92(0.26)	14.81(0.41,0.21)	7.98(0.48,0.23)	19.32(0.53,0.27)

blurred both by the time resolution of the diagnostic and the presence of a 1–3- $\mu\text{m}$  glue layer between the aluminum and quartz. Determining  $U_s^{\text{Al}}(t_{\text{bo}})$  requires estimation of the time history,  $U_s^{\text{Al}}(t)$ . This can be achieved using the measured  $U_s^{\text{Q}}(t)$ , given that the same pressure source drives both materials in parallel. Since aluminum and quartz have such similar impedances, to a good approximation  $U_s^{\text{Al}}(t) - \langle U_s^{\text{Al}} \rangle = U_s^{\text{Q}}(t) - \langle U_s^{\text{Q}} \rangle$ , provided the average for both materials is taken over the same time period (the step transit time in this case).<sup>31</sup> Although the absolute quartz velocity has a 1%–2% error, the uncertainty in  $U_s^{\text{Q}} - \langle U_s^{\text{Q}} \rangle$  is smaller, usually less than 1% of the velocity if the shock velocity varies smoothly. This error is summed in quadrature with the other errors in both  $U_s^{\text{Q}}$  and  $U_s^{\text{Al}}$ .

The aluminum and quartz shock velocities are plotted in Fig. 2 and tabulated in Table I. The best linear fit to the data, expressed in a form where errors in the coefficients are independent, is given by  $U_s^{\text{Al}} = B_0 + B_1(U_s^{\text{Q}} - \overline{U_s^{\text{Q}}})$  where  $\overline{U_s^{\text{Q}}} = 20.57$ ,  $B_0 = 21.14 \pm 0.12$ , and  $B_1 = 0.91 \pm 0.03$ .

Having extracted  $U_s^{\text{Al}}$  and  $U_s^{\text{Q}}$  at the interface, impedance matching can now be applied to determine the quartz pressure, density, and particle speed. This requires knowledge of the aluminum Hugoniot and its release isentropes. There are two approaches to determining these. The first method uses a model EOS for aluminum, usually in the form of a table. This assures thermodynamic consistency in the calculations but makes it difficult to rigorously account for errors in the EOS model, a factor that becomes crucial at multimegabar pressures. The second method, which we use here, relies on the approximation that release curves are simply a reflection of the Hugoniot about the initial shock state in the pressure-particle velocity ( $P$ - $U_p$ ) plane.<sup>10</sup> Since the Hugoniot of aluminum (and many other materials) can be described by a linear fit in  $U_s$ - $U_p$  the great advantage of this approach is that the fit uncertainties give a direct way to estimate *systematic* errors in the aluminum EOS.<sup>32</sup> A possible drawback to this technique is that it does not automatically assure thermodynamic consistency between the different Hugoniots and isentrope combinations. This is unlikely to be a problem for such small variations in the Hugoniot and isentrope. The impedance match results, using a fit to absolute aluminum data given by  $U_s = 6.591 + 1.157U_p$ ,<sup>33</sup> are shown in Table I with both the random and systematic errors given in parentheses. Random errors are a direct result of the listed velocity measurement errors, while systematic errors are the result of errors in the aluminum EOS. Note how the systematic uncertainties are always smaller than the random uncertainties but rise to a third of the total error at the highest pressure near  $\sim 15$  Mbars.

#### IV. DISCUSSION

These data, along with the results from earlier studies, are plotted in the  $U_s$ - $U_p$  plane in Fig. 3, with the best linear fit, given by  $U_s = 4.08 + 1.30U_p$ , and its associated uncertainties shown as three dashed lines.<sup>34</sup> The fit is in good agreement with the previous data from Trunin *et al.*<sup>15</sup> and Trunin<sup>16</sup> for  $13 < U_s < 20 \mu\text{m/ns}$  and extrapolates to the nuclear-driven point at  $U_s = 33 \mu\text{m/ns}$ . The scatter in our data is

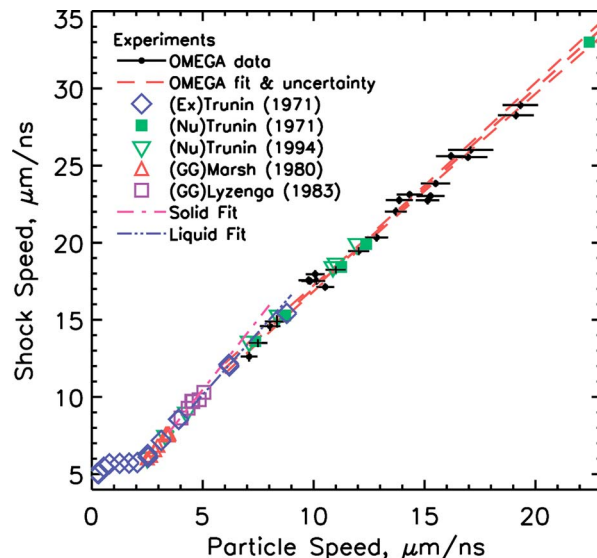


FIG. 3. (Color online) Measured quartz Hugoniot shown in the shock velocity vs particle velocity plane. The red dashed lines give the best linear fit and associated  $1\sigma$  uncertainty to the data from this study (black circles with error bars). Previous data from Trunin *et al.* (Ref. 15) and Trunin (Ref. 16) performed on explosively driven (Ex) and nuclear-driven (Nu) platforms are in good agreement with those from this study to within experimental uncertainties. Selected data at lower pressures obtained on gas gun experiments (GG) are also shown from Lyzenga and Ahrens (Ref. 9) and Marsh (Ref. 35). Linear fits determined by Lyzenga and Ahrens (Ref. 9) are shown for the solid (stishovite- or stishovite-like) phase (pink, dot-dash line) and the liquid phase (dark blue, double-dot-dash line) immediately after melting.

consistent with the quoted errors, giving a reduced  $\chi^2 = 1.2$  (systematic errors due to the aluminum EOS, which do not contribute to the data scatter, are not included in the  $\chi^2$  calculation). Errors in the data from Trunin<sup>16</sup> are not provided for each shot but are quoted to be about 2% at the highest pressures, very similar to those for our measurements. These results show that to better than 2% in shock velocity, our data, achieved on time scales of less than 1 ns, are in agreement with the data achieved on time scales up to tens of microseconds.

By comparing the data from earlier sources that have investigated compression in the solid phases through the onset of melting at 1 Mbar (Refs. 9,15,16,35) the trend toward softening of the Hugoniot becomes apparent. It is seen most clearly by comparing the slopes of the linear  $U_s$ - $U_p$  fits in different pressure regimes (see Figs. 3 and 4). In the high-pressure solid up to melt, the data follow  $U_s = 1.370 + 1.822U_p$  (Ref. 9); in the liquid immediately above melt the best fit gives  $U_s = 2.049 + 1.619U_p$  (Ref. 9); merging into the dense plasma our data give a fit of  $U_s = 4.08 + 1.30U_p$  over an extensive pressure range. The slope  $S = dU_s/dU_p$  is thus decreasing with pressure. The use of piecewise linear fits is only a convenient construction and the actual Hugoniot is likely to smoothly transition to the gentler slope over a finite pressure range between 1 and  $\sim 4$  Mbars. Different regimes along the quartz Hugoniot can thus be roughly characterized as (1) solid for  $P \leq 1$  Mbar, (2) liquid for  $1 \leq P \leq 4$  Mbars, and (3) dense plasma for  $P \geq 4$  Mbars. The softening of the Hugoniot above 1 Mbar was described theoretically by Kerley<sup>36</sup> who showed that without including the effects of



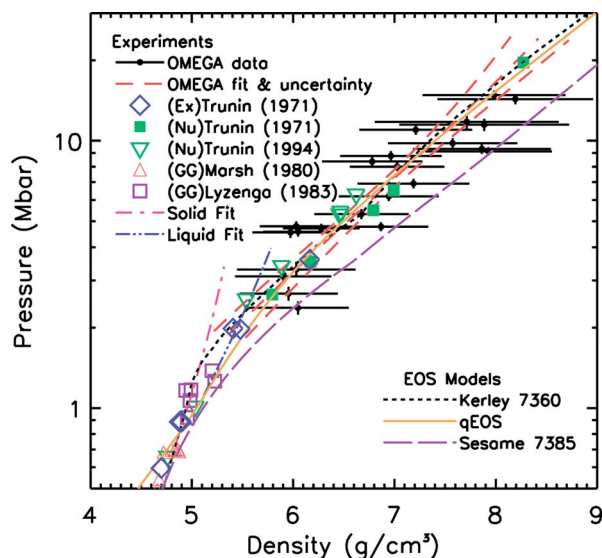


FIG. 4. (Color online) Measured quartz Hugoniot from Fig. 3 in the pressure-density plane illustrating the softening of the quartz Hugoniot as it proceeds through melt to the liquid and dense plasma phases. Predictions of some EOS models are shown for comparison. As in Fig. 3, previous data from explosive (Ex), nuclear (Nu), and gas gun (GG) experiments are shown and are in good agreement with the laser-driven data from this study.

dissociation the quartz Hugoniot continued to follow the less compressible path given approximately by the liquid fit in our plot; including dissociation caused a suppression of the temperature at a few megabars (as a result of the dissociation energy) and a resultant softening of the Hugoniot. A recent molecular-dynamics simulation has also shown that in the pressure range between 1 and 5 Mbars silica undergoes a loss of coordination between Si and O atoms,<sup>17</sup> a process characteristic of dissociation in the dense fluid.

The data are compared to models by plotting them in the  $P$ - $\rho$  plane in Fig. 4. Although the SESAME (Ref. 37) model is in poor agreement with the best fit to our data, both the Kerley<sup>36</sup> and quotidian equation of state<sup>38</sup> (qEOS) models are in good agreement. It is important to note that these models achieve similar  $P$ - $\rho$  behavior despite having significantly different temperature behaviors. The explicit inclusion of dissociation effects by Kerley<sup>36</sup> causes a lowering of temperature, an effect not observed in qEOS. Note that both these models do not agree with the data in the vicinity of the melt at 1 Mbar, a disagreement possibly caused by the observed superheating of the solid phase.<sup>9</sup>

It is instructive to examine how the Grüneisen parameter,  $\Gamma$ , changes along the quartz Hugoniot. In stishovite,  $\Gamma$  has been determined by comparing the principal Hugoniot of quartz, coesite, and stishovite,<sup>14</sup> and is found to decrease with volume to 0.7 near the melting point, having dropped from 1.35 at ambient pressure. At higher pressures we can approximate  $\Gamma$  from the slope,  $S$ , of our data by the simple relation  $\Gamma \approx 2(S-1)$ .<sup>39</sup> This is rigorously true in the limit of maximum compression (when neighboring states on the Hugoniot are isochoric) but was found to be approximately valid even at considerably lower pressures such as those down to several megabars.<sup>39</sup> Since  $S=1.30$  between 2 and 15 Mbars it appears that, within the validity of this approxima-

tion,  $\Gamma \approx 0.6$  over this wide range. It is noteworthy that experiments comparing the Hugoniot for quartz with that for porous samples estimated  $\Gamma=0.6 \pm 0.1$  (Refs. 10 and 16) for fluid silica while available EOS models give  $\Gamma \approx 0.5-0.7$  (Refs. 36 and 38) in this high-pressure range. This indicates that  $\Gamma$  drops rapidly during initial compression in the solid phase but reaches an approximately constant value at pressures just above the melt transition with dissociation at a few megabars causing little effect.<sup>40</sup> It is not until pressures exceed 100 Mbars that inner-shell ionization begins to cause  $\Gamma$  to decrease below 0.6.

## V. CONCLUSIONS

An extensive study has been performed on shocked silica in the regime where it transforms from a liquid near melt to a dense plasma. Three regimes have been identified: solid ( $P \leq 1$  Mbar), dissociating liquid ( $1 \leq P \leq 4$  Mbars), and dense plasma ( $P \geq 4$  Mbars). The softening of the Hugoniot between 1 and 4 Mbars is likely caused by dissociation of the Si-O system. With these laser-driven shock wave measurements on quartz an accurate comparison can now be made between three different experimental platforms all attempting to achieve the same thermodynamic states with time scales spanning over four orders of magnitude. In the region between 2 and 6 Mbars, where results from all platforms exist, the data from explosive-driven, nuclear-driven, and laser-driven experiments all produce the same results within experimental errors. Although extensive experiments have shown that quartz exhibits nonequilibrium behavior at both solid-solid<sup>23</sup> and solid-liquid<sup>9</sup> phase boundaries, once the fluid phase has been accessed the shock states achieve equilibrium in significantly less than a nanosecond.

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## APPENDIX: DEVELOPMENT OF QUARTZ AS AN IMPEDANCE-MATCH STANDARD

The impedance-matching technique for determining a material's Hugoniot is a relative EOS measurement whose reliability ultimately rests on the precision to which the EOS of the standard is known. Aluminum is the most often used standard since it has the largest number of absolute Hugoniot measurements<sup>22,41</sup> over a wide range of pressures, particularly in the regime of one to tens of megabars currently the focus of laser-driven,<sup>42,43</sup> explosively driven,<sup>44</sup> and magnetically driven<sup>45</sup> shock techniques.

The development of the VISAR technique in laser-driven shock experiments<sup>27,28</sup> has allowed shock speed measurements with  $\sim 1\%$  precision to be achieved and enabled

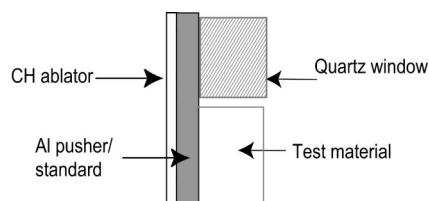


FIG. 5. (Color online) A new, high-precision scheme for determining aluminum shock velocities in an impedance-match experiment. In this arrangement, the VISAR-measured shock velocity in the quartz window is used to infer the shock velocity in aluminum prior to breakout, the relationship between aluminum and quartz shock velocities being given by the statistically averaged fit shown in Fig. 2 and provided in the text. This significantly reduces the error arising from transit-time measurements across a step.

continuous recording of the shock velocity with time in *transparent* materials. In an opaque material such as aluminum, however, the VISAR cannot be used and shock speeds must be obtained from the transit time across a known step height, an inherently less precise measurement (see the discussion in Sec. III). Since the impedance-matching calculation further magnifies errors in the shock velocity of the standard, the uncertainties in  $U_s^{\text{Al}}$  are very often the dominant component of the final errors in  $\rho$  and  $U_p$ . With the extensive Hugoniot measurements obtained in this study it now becomes possible to replace aluminum with quartz to take advantage of the increased measurement precision of the VISAR. This should significantly improve the accuracy of future impedance-matching measurements at least to the extent that the release or reshock states are well approximated by the reflected Hugoniot.<sup>32,46</sup>

For experiments with a large impedance mismatch, in which the reflected Hugoniot approximation breaks down, knowledge of the release curve (or reshock Hugoniot) is required in addition to the principal Hugoniot determined in this study. However, experimental data on the release of quartz are thus far limited to first shock states below 1 Mbar,<sup>47</sup> in contrast the limit for aluminum is up to  $\sim 5$  Mbars.<sup>48</sup> Systematic errors in the off-Hugoniot states of quartz are thus likely to be difficult to quantify, potentially offsetting the benefits of a more precise shock velocity measurement.<sup>49</sup> For such a situation we have developed a new technique that takes advantage of the increased measurement precision in the quartz sample while still relying on aluminum as the material standard. In this new scheme, a quartz “window,” identical to the sample used in these experiments, would be mounted on half a *flat* aluminum pusher, as shown in Fig. 5, with the other half being covered by the test sample. The shock speed in aluminum immediately prior to breakout can then be determined by measuring the shock speed in quartz immediately after breakout and using the linear relation shown in Fig. 2 and provided in the text. Such a scheme has recently been used to study the principal Hugoniot of liquid deuterium.

For measurements of the double-shock behavior of liquid deuterium, quartz has already been used as an anvil.<sup>50</sup> In this configuration only knowledge of the principal Hugoniot is required. The precise fit for quartz was slightly different to that given in this paper since that earlier study used a pre-

liminary set of quartz data. These differences are negligible and do not affect the results from that study.

In the schemes just described, the central principal is to develop a transparent standard for performing measurements as close as possible to the impedance-matching interface. Localizing the measurement in both space and time minimizes any effects due to spatial or temporal variations in the shock wave and eliminates the need for a transit-time measurement. This approach can only grow in importance as higher pressures are accessed.

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- <sup>30</sup>Note that this time is smaller than the instrument resolution of 40–50 ps which is a product of the VISAR delay (16 or 37 ps for the etalons used in this case) and streak camera convolution and is a measure of the smallest clearly distinguishable time between two events. This is possible since the separation between breakout events is much greater than the instrument resolution and the data record is oversampled (with  $\sim 15$  pixels per resolution element in this case).
- <sup>31</sup>Corrections for shock unsteadiness in the past have usually relied on two calculations: a hydrodynamic simulation of the experiment, and an assumed EOS for the material under study (see Refs. 10, 15, and 16). Our

approach removes the need for a hydrodynamic simulation—since we are able to measure the adjacent shock velocity in quartz—but still relies on prior information about the EOS of quartz (which we have simply assumed to be similar to aluminum).

- <sup>32</sup>Higher-order corrections to account for the slight deviation of the release isentrope from its reflected Hugoniot approximation are generally negligible unless release pressures are less than a third of the original pressure at the Hugoniot (see Ref. 46). Since quartz is close in impedance to aluminum this is not a concern here. For completeness these deviations were estimated by averaging the predictions from several EOS models and deriving a composite release *correction curve*. This small correction and its uncertainty (given by the scatter between models) were then added to the reflected experimental Hugoniot. Although this makes the release curve model dependent, the contributions of the models are very small. For the aluminum-quartz combination this correction is negligible. This procedure will be described in detail in a future publication by Celliers *et al.* and is of particular relevance to low impedance materials.
- <sup>33</sup>The fit to the aluminum Hugoniot with associated errors was found to be  $U_s = a_0 + a_1[U_p - \bar{U}_p]$  where  $a_0 = 17.409 \pm 0.081 \mu\text{m/ns}$ ,  $a_1 = 1.157 \pm 0.031$ , and  $\bar{U}_p = 9.3502 \mu\text{m/ns}$ . This was obtained by fitting published absolute data (Refs. 22 and 41) as well as some recent unpublished points provided by M. D. Knudson (private communication).
- <sup>34</sup>Since the errors in  $U_p$  for the quartz Hugoniot are significantly larger than those in  $U_s$ , the fit was performed with  $U_p$  as the dependent variable and found to be  $U_p = C_0 + C_1(U_s - \bar{U}_s)$ , where  $\bar{U}_s = 20.57 \mu\text{m/ns}$  was the mean shock velocity for all the shots,  $C_0 = 12.74 \pm 0.12 \mu\text{m/ns}$  and  $C_1 = 0.772 \pm 0.027$ .
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